

$$m_1 v_1' + m_2 v_2' = m_1 v_1 + m_2 v_2 \quad \textcircled{1}$$

$$-v_1' + v_2' = e(v_1 - v_2) \quad \textcircled{2}$$

$$\textcircled{1} - m_2 \times \textcircled{2}$$

$$\begin{aligned} (m_1 + m_2)v_1' &= m_1 v_1 + m_2 v_2 - m_2 e(v_1 - v_2) = m_1 v_1 + m_2 v_1 - m_2 v_1 + m_2 v_2 - m_2 e(v_1 - v_2) \\ &= (m_1 + m_2)v_1 - m_2(1 + e)(v_1 - v_2) \end{aligned}$$

$$\therefore v_1' = v_1 - \frac{m_2}{m_1 + m_2}(1 + e)(v_1 - v_2)$$

$$\textcircled{1} + m_1 \times \textcircled{2}$$

$$\begin{aligned} (m_1 + m_2)v_2' &= m_1 v_1 + m_2 v_2 + m_1 e(v_1 - v_2) = m_1 v_1 + m_1 v_2 - m_1 v_2 + m_2 v_2 + m_1 e(v_1 - v_2) \\ &= (m_1 + m_2)v_2 + m_1(1 + e)(v_1 - v_2) \end{aligned}$$

$$\therefore v_2' = v_2 + \frac{m_1}{m_1 + m_2}(1 + e)(v_1 - v_2)$$